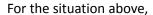
Learning Team Activity: Compare/Contrast Models

Bathtub Model: $X' = 10 - 0.2X$	Logistic Growth Model: $X' = bX - cX^2$
Shark-Tuna model: $T' = -\beta ST + b_T T$ $S' = m\beta ST - d_S S$	

- 1. Find the outflow terms in each model. Mark these in red. How did you identify the outflow terms?
- 2. Find the inflow terms in each model. Mark these in blue. How did you identify the outflow terms?
- 3. Find the parameters in each model. Mark these in green. How did you identify the outflow terms?
- 4. Find the terms that show state variables interacting with one another. Mark these in yellow. How did you identify the outflow terms?

Class Activity: Eucalyptus & Koalas

- 5. Koalas (*K*) feed exclusively on eucalyptus (*E*). Use the following assumptions to write a differential equation model of the food chain.
 - (1) Eucalyptus grows at a per-biomass (like per-capita) rate of 0.01.
 - (2) Due to shading, the per-biomass rate at which eucalyptus dies is proportional to the amount of eucalyptus with a proportionality constant of 0.02.
 - (3) Koalas consume eucalyptus at a per-capita rate proportional to the amount of eucalyptus available, with a proportionality constant of 0.05.
 - (4) The koala birth rate is proportional to the amount of eucalyptus they consume, with a proportionality constant of 0.15.
 - (5) Koalas die at a per-capita rate of 0.03



- a. Identify the state variable(s).
- b. Sketch a box-and-arrow diagram. Draw in all the connections, but if the connection is not a direct flow from one box to another with the same numbers, use a dotted line.
- c. Write a differential equation model



Learning Team Activity: Ants and Aphids

- 6. Ants and aphids have a well-documented relationship, as described below. Set up a differential equation model for the populations of ants (N) and aphids (P), based on the following assumptions:
 - (1) The aphids secrete a sugary substance called honeydew, which provides a food source for the ants. Therefore, the per-capita birth rate of the ants is proportional to the aphid population, with a proportionality constant of 0.03.
- viamoi, CC BY 2.0, via Wikimedia Commons

- (2) 2% of the ants die per day.
- (3) The aphids have a per-capita birth rate of 12% per day.
- (4) Due to crowding, the per-capita death rate of the aphids is proportional to the aphid population, with proportionality constant 0.001.
- (5) Aphids can also be killed by predators, but to protect their source of honeydew, the ants will aggressively defend the aphids: the more ants there are, the lower the risk of predation for the aphids. Thus, the per-capita predation rate for aphids is proportional to the inverse of the ant population, with a proportionality constant of 0.7.

For the mathematical model above,

- a. Identify the state variable(s)
- b. Sketch a box-and-arrow diagram. Draw in all the connections, but if the connection is not a direct inflow or outflow, use a dotted line. (Like we did with feedback diagrams.)
- c. Write a differential equation model