

### Quiz 3

Name:

1. Let  $V$  and  $W$  be finite dimensional vector spaces with an one-to-one linear transformation  $T : V \rightarrow W$ . Prove that  $\dim V \leq \dim W$ . (Hint: If  $X$  is a vector space with  $\dim X = n$  then any linearly independent subset of  $X$  must have cardinality less than  $n$ .)

2. Let  $V$  and  $W$  be finite dimensional vector spaces with an onto linear transformation  $T : V \rightarrow W$ . Let  $S$  be any spanning set of  $V$ . Prove that  $T(S) = \{T(s) : s \in S\}$  is also spanning.